

Key

Name: _____

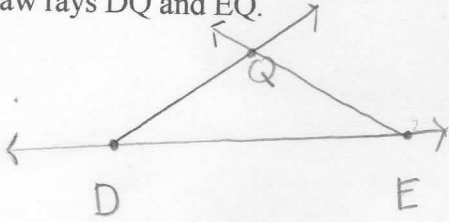
Period: _____

Date: _____

Line, segment, and ray homework

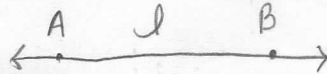
Answer all questions with a complete sentence.

- a. Draw two points, D and E. Then draw line DE.
b. Draw point Q not on the line.
c. Draw rays DQ and EQ.



2. What are three possible names for the line shown?

\overleftrightarrow{AB} \overleftrightarrow{BA} \overleftrightarrow{J}



3. Can the ray shown be called XY? Why not?



The name starts with point at end.

4. According to the definition of a line found on GFEC text found on page 3, a line is made up of what?

Points.

- a. Does this agree or disagree with Euclid? Provide examples from texts to support your claim.

Do # 10 b. on p 15 and # 13 & 14 on p 16 of GFEC below

10b. The length of \overline{PQ} is 5 units.

If R is at 7 and Q is at 3, the length of

\overline{QR} would be 4 units

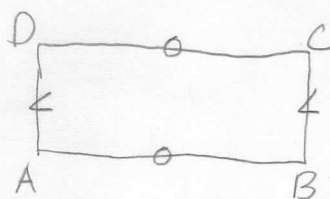
4 units \neq 5 units

$\overline{QR} \neq \overline{PQ}$ (substitution)

13. Perimeter of $ABDC = 66$

$$\overline{DC} = 2\overline{CB}$$

How long is AB ?



What can we write from the information that has been given?

$$\frac{1}{2}\overline{DC} = \overline{CB} \quad \text{Algebraic division}$$

$$\overline{DC} \cong \overline{AB} + \overline{AB} \quad \text{Given in diagram}$$

$$\overline{DC} = \overline{AB} + \overline{AB} \quad \text{Definition of congruent}$$

$$\frac{1}{2}\overline{DC} = \frac{1}{2}\overline{AB} + \frac{1}{2}\overline{AB} \quad \text{Algebraic division}$$

$$\overline{CB} \cong \overline{AD} \quad \text{Given in diagram}$$

$$\overline{AD} = \frac{1}{2}\overline{AB} \quad \text{Euclid C.N. 1}$$

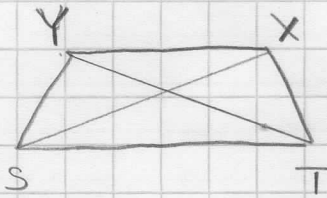
$$\text{Perimeter} = \overline{DC} + \overline{CB} + \overline{AB} + \overline{AD}$$

$$66 = \overline{AB} + \frac{1}{2}\overline{AB} + \overline{AB} + \frac{1}{2}\overline{AB} \quad \text{substitution}$$

$$66 = 3\overline{AB}$$

$$\boxed{33 = \overline{AB}} \quad \text{Algebraic division}$$

14.



$$\overline{XS} = \overline{YT}$$

solve for r and m

$$\overline{YS} = \overline{XT}$$

$$\overline{XT} = 2r + 5$$

$$2r + 5 = 3.5r + 2$$

$$\overline{XS} = 3m + 7$$

$$3 = 1.5r$$

$$\overline{YS} = 3\frac{1}{2}r + 2$$

$$\boxed{2 = r}$$

$$\overline{YT} = 4.2m + 5$$

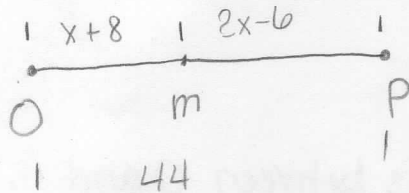
$$4.2m + 5 = 3m + 7$$

$$1.2m = 2$$

$$\boxed{m = 1.6}$$

Collinear, noncollinear, between, bisector and congruence homework

1. Point M is between endpoints O and P on line segment OP. $OM = x + 8$; $MP = 2x - 6$; $OP = 44$ Solve the length of both OM and MP and determine if point M bisects line segment OP.



$$x + 8 + 2x - 6 = 44$$

$$3x + 2 = 44$$

$$3x = 42$$

$$x = 14$$

$$OM = MP$$

$$\overline{OM} = x + 8 = 14 + 8 = 22$$

$$\overline{MP} = 2x - 6 = 2(14) - 6$$

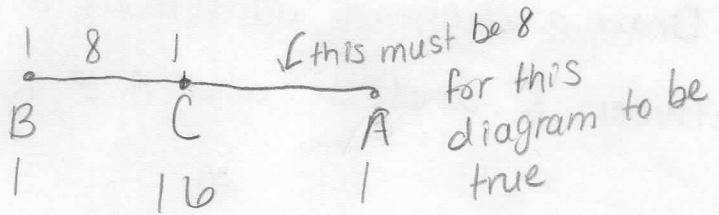
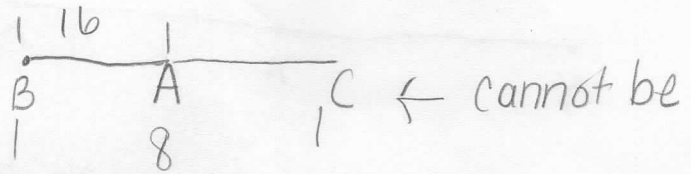
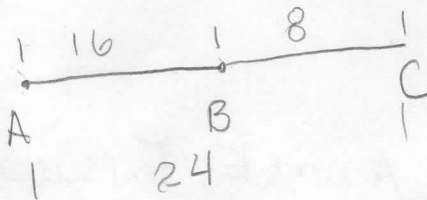
$$= 28 - 6$$

$$= 22$$

$\therefore M$ Bisects \overline{OP}

2. If $AB = 16$, $BC = 8$, and $AC = 24$, which point is between?

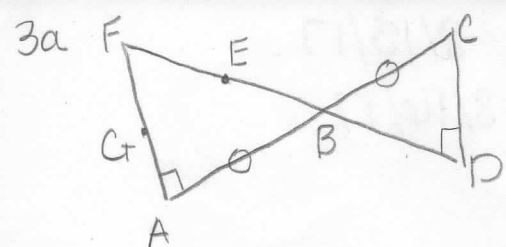
a. Draw three diagrams. Draw one that proves the point between and draw two showing that the other points cannot be between.



3. Draw a number line and shade all points that are at or between -5 and 2. Write the length of this shaded segment.



length = 7 units



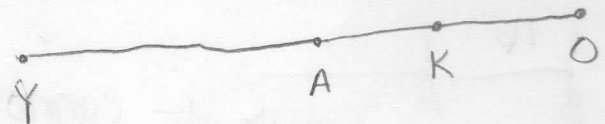
name all pts that are collinear with E & F

B, D

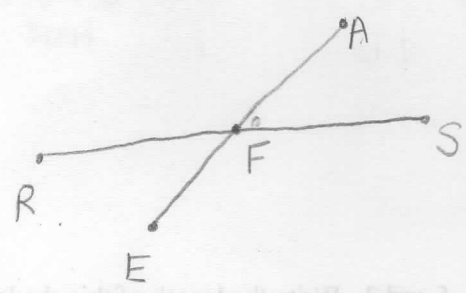
b. Are G, E, and D collinear? No

Are F and C collinear? Yes

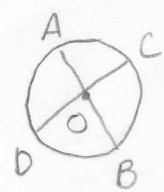
10. A, K, O, and Y are collinear points. K is between O and A. The length of \overline{AO} added to the length of \overline{AY} is equal to the length of \overline{OY} . A is to the right of O



11. Draw a diagram in which F is between A and E. F is also between R and S and A, E, R, and S are non-collinear.



1. a

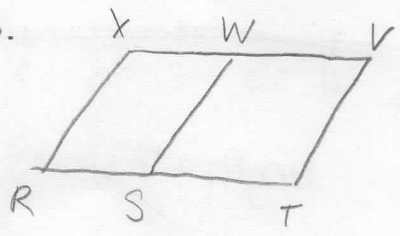


O is midpoint of \overline{AC}

Name all congruent segments

$$\overline{DO} \cong \overline{OC}$$

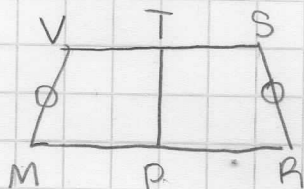
b.



\overline{SW} Bisects \overline{RV}

$$\overline{XW} \cong \overline{WV}$$

19.

Given: \overleftrightarrow{TP} bisects \overline{VS} and \overline{MR}

$$\overline{VM} \cong \overline{SR}$$

$$\overline{MP} = 9, \overline{VT} = 6$$

perimeter of $MRSV = 62$ Find VM

why

$$\overline{VT} = \overline{TS}$$

$$\text{and } \overline{MP} = \overline{PR}$$

def. of bisector

$$\overline{VM} = \overline{SR} \quad \text{def. of congruence}$$

$$\text{perimeter} = \overline{VT} + \overline{TS} + \overline{SR} + \overline{PR} + \overline{MP} + \overline{VM}$$

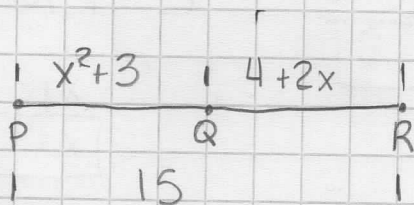
$$62 = 6 + 6 + \overline{VM} + 9 + 9 + \overline{VM}$$

Substitution

$$32 = 2\overline{VM}$$

$$\boxed{16 = \overline{VM}}$$

21.

a. Find the value of x

$$x^2 + 3 + 4 + 2x = 15$$

$$x^2 + 2x - 8 = 0$$

$$(x + 4)(x - 2) = 0$$

$$x \neq -4$$

$$\boxed{x = 2}$$

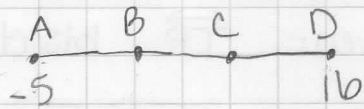
b. Is Q the midpoint of \overline{PR} ?

$$x^2 + 3 = 4 + 3 = 7$$

$$4 + 4 = 8$$

$$\boxed{\text{No}}$$

5.



B and C trisect \overline{AD}

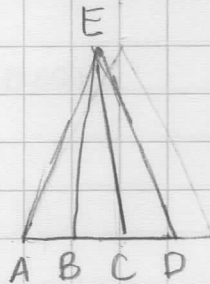
a. Find the coordinates of B and C

$$\boxed{B=2 \quad C=9}$$

b. Find \overline{AC}

$$\boxed{\overline{AC} = 14}$$

8 a.



B and C are trisection points of \overline{AD} and $\overline{AD} = 12$

a. Find \overline{AB}

$$\boxed{\overline{AB} = 4}$$

b. Find \overline{AC}

$$\boxed{\overline{AC} = 8}$$

c. If $\overline{AB} = x + 3$, solve for x

$$x + 3 = 4$$

$$\boxed{x = 1}$$

d. If $\overline{AB} = x + 3$ and $\overline{AE} = 3x + 6$, find AE

$$x = 1 \quad \overline{AE} = 3(1) + 6$$

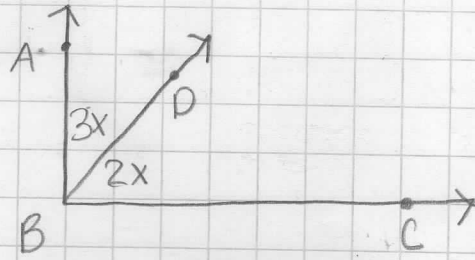
$$\boxed{\overline{AE} = 9}$$

e. What segment is C the midpoint of?

$\boxed{C \text{ is the midpoint of segment } BD.}$

P21

6.



$\angle ABC$ is a right angle. The ratio of the measures of $\angle ABD$ and $\angle DBC$ is 3 to 2. Find measure of $\angle ABD$

$$3x + 2x = 90^\circ$$

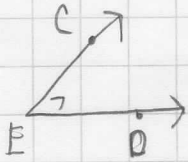
$$5x = 90^\circ$$

$$x = 18^\circ$$

$$\angle ABD = 3x = 3(18^\circ) = \boxed{54^\circ}$$

p7

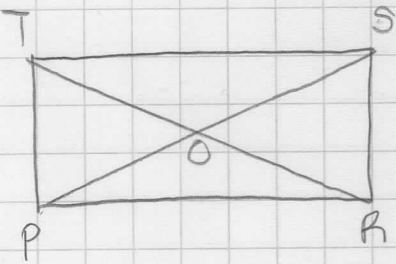
2



What are 4 possible names for the angle shown?

$\angle CED, \angle DEC, \angle E, \angle 7$

6



a) Name $\angle OPR$ in all other possible ways

$\angle SPR, \angle RPO, \angle RPS$

b) What is the vertex of $\angle TOS$?

The vertex of $\angle TOS$ is O

c) How many angles has vertex R?

Vertex R has 2 angles

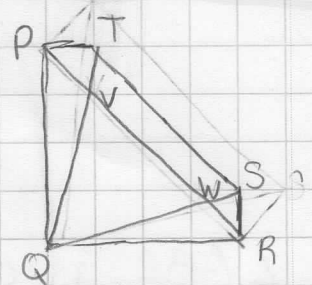
d) Name $\angle TSP$ in all other possible ways.

$\angle TSO, \angle PST, \angle OST$

p14-15

4e

Honors Geometry HW Ke
Assigned 8-16-17
Due 8-17-17



How many angles have vertex Q?

Vertex Q has 6 angles

←

b) There is a right angle at each corner of PRST.

a) If $\angle TPO = 60^\circ$ how large is $\angle RPO$?

$\angle RPO = 30^\circ$

b) If $\angle PTO = 70^\circ$, How large is $\angle STO$?

$\angle STO = 20^\circ$

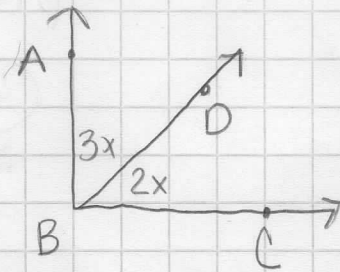
c) If $\angle TOP = 50^\circ$, how large is $\angle POR$?

$\angle POR = 130^\circ$

d) Classify $\angle TOS$ as acute, right, or obtuse

$\angle TOS = 130^\circ$
so $\angle TOS$ is obtuse

p 21



$\angle ABC$ is a right angle. The ratio of the measures of $\angle ABD$ and $\angle DBC$ is 3 to 2. Find $\angle ABD$

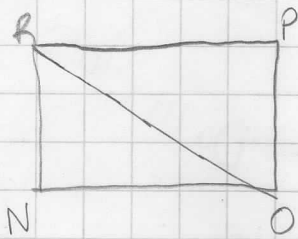
$$3x + 2x = 90^\circ$$

$$5x = 90^\circ$$

$$x = 18^\circ$$

$$\begin{aligned}\angle ABD &= 3x \\ &= 3(18^\circ) \\ &= 54^\circ\end{aligned}$$

2



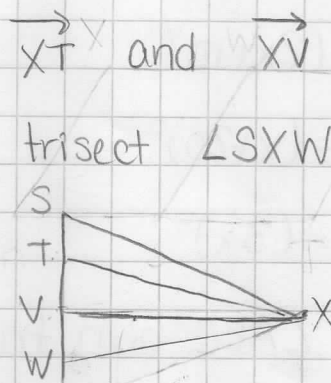
(a)

\vec{RO} bisects $\angle NRP$

Name the congruent angles.

$\angle NRO \cong \angle ORN$ } these are the same \angle , just have the letters arranged different
 $\angle ORP \cong \angle PRO$ } same

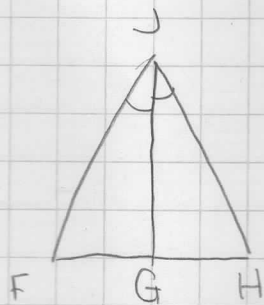
(b)



$\angle SXT \cong \angle TXS$
 $\angle TXV \cong \angle VTX$
 $\angle VXW \cong \angle WXV$

3

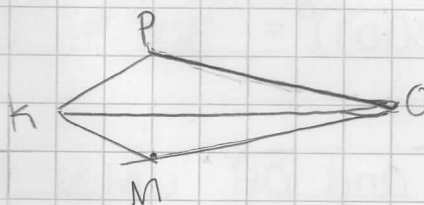
(a)



Name the angle bisector

\vec{JG}

(b)



$\angle POK \cong \angle MOK$

\vec{OK}

7. Given: $\angle FGJ = 3x - 5$
 $\angle JGH = x + 27$

\vec{GJ} bisects $\angle FGH$

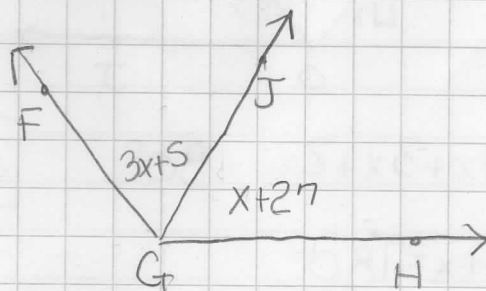
Find $\angle FGJ$

$\angle FGJ = \angle JGH$

$3x - 5 = x + 27$

$2x = 32$

$x = 16$



why
 definition of angle bisector

substitution

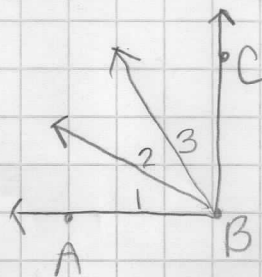
$\angle FGH = 3(16) - 5 = 43$
 $\angle JGH = 16 + 27 = 43$

9. Given: $\angle ABC = 90^\circ$

$$\angle 1 = (2x + 10)^\circ$$

$$\angle 2 = (x + 20)^\circ$$

$$\angle 3 = (3x)^\circ$$



Do in class

Has $\angle ABC$ been trisected?

Yes, $\angle ABC$ has been trisected

$$2x + 10 = x + 20$$

$$x = 10$$

$$\angle 1 = [2(10) + 10]^\circ = [20 + 10]^\circ = 30^\circ$$

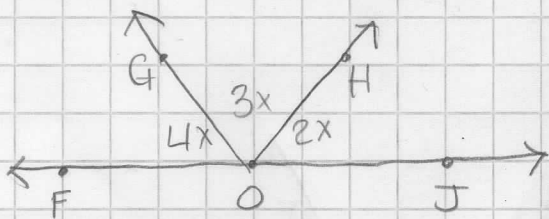
$$\angle 2 = (10 + 20)^\circ = 30^\circ$$

$$\angle 3 = (3(10))^\circ = 30^\circ$$

18. \vec{OG} and \vec{OH} divide straight angle $\angle FOJ$

into three angles whose measures are in the ratio of

4:3:2 Find $\angle FOG$



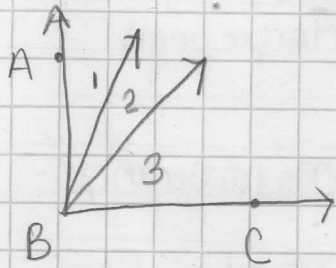
$$4x + 3x + 2x = 180^\circ$$

$$\angle FOG = 4(20^\circ) = 80^\circ$$

$$9x = 180^\circ$$

$$x = 20^\circ$$

11. $\overleftrightarrow{AB} \perp \overleftrightarrow{BC}$ and angles 1, 2, and 3 are in the ratio 1:2:3. Find the measure of each angle.



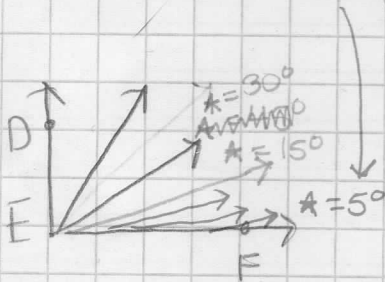
$$1x + 2x + 3x = 90^\circ$$

$$6x = 90^\circ$$

$$x = 15^\circ$$

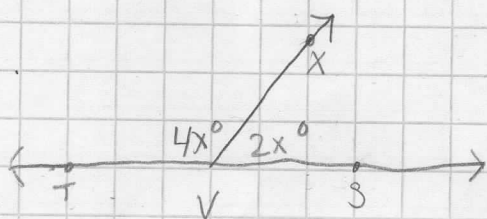
$\angle 1 = 1x = 15^\circ$ $\angle 2 = 2x = 30^\circ$ $\angle 3 = 3x = 45^\circ$
--

12. Line DE is perpendicular to line EF. *The resulting angle is trisected* then one of the new angles is bisected, and *then one of the resulting angles is trisected. How large is the smallest angle? Give answer in degrees.



P. 70

10. Find the measure of $\angle XVS$



$$4x^\circ + 2x^\circ = 180^\circ$$

$$6x^\circ = 180^\circ$$

$$x = 30^\circ$$

$$\angle XVS = 2x^\circ = 2(30)^\circ = \boxed{60^\circ}$$

11. One of two supplementary angles is 70° greater than the second. Find the measure of the larger angle.

$$x^\circ + x^\circ + 70^\circ = 180^\circ$$

$x^\circ =$ smaller angle
 $x^\circ + 70^\circ =$ larger angle

$$2x^\circ + 70^\circ = 180^\circ$$

$$2x^\circ = 110^\circ$$

$$x^\circ = 55^\circ$$

$$x^\circ + 70^\circ = \text{larger angle}$$

$$55^\circ + 70^\circ = \text{larger } \angle$$

$$125^\circ = \text{Large } \angle$$

16. Two supplementary angles are in the ratio 11:7
find the measure of each.

$$7x + 11x = 180^\circ$$

$$18x = 180^\circ$$

$$x = 10^\circ$$

$$7x = 70^\circ$$

$$11x = 110^\circ$$

Honors Gem HW key
Assigned 8/18/17
due 8/23/17

P 14-17

1 Change to Deg. & Min.

a) $61\frac{2}{3}^\circ$

$61^\circ 40'$

b) 71.7°

$71\frac{7}{10}^\circ$

$71^\circ 42'$

2 Change to Deg.

a) $132^\circ 30'$

$132\frac{30}{60}^\circ$
 $132\frac{1}{2}^\circ$
 132.5°

b) $19^\circ 45'$

$19\frac{45}{60}^\circ$
 $19\frac{3}{4}^\circ$
 19.75°

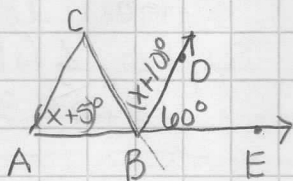
5. $49^\circ 32' 55''$
 $+ 37^\circ 27' 15''$
 $87^\circ 60' 10''$

$87^\circ 60' 10''$

b) $123^\circ 15'$
 $- 40^\circ 26'$

$122^\circ 75'$
 $- 40^\circ 26'$
 $82^\circ 49'$

8. IF $\angle CBD \cong \angle DBE$ Find $\angle A$

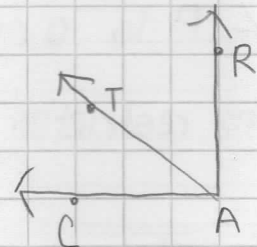


$(x+10)^\circ = 60^\circ$

$x^\circ = 50^\circ$

$\angle A = x^\circ + 5^\circ$
 $= 50^\circ + 5^\circ$
 $= 55^\circ$

11.



Given: $\angle CAR$ is a right angle

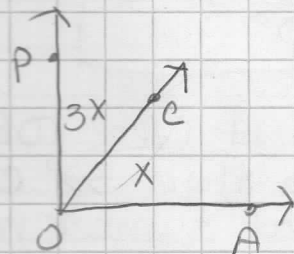
$\angle CAT = 37^\circ 66' 10''$

find $\angle RAT$

$88^\circ 119' 60''$
 $- 37^\circ 66' 10''$
 $51^\circ 53' 50''$

16. IF $\angle POA$ is a

right angle and if $\angle POC$ is 3x as large as $\angle COA$, find $\angle POC$

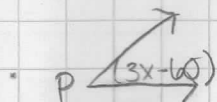


$4x = 90^\circ$
 $x = 17\frac{1}{2}^\circ$ or 17.5°

$3x = 52.5^\circ$

(17) $\angle P$ is acute what are

(a) its restrictions?



$$0 < 3x-60 < 90$$

(b) what are the restrictions on x

$$60^\circ < 3x < 150^\circ$$

$$20^\circ < x < 50^\circ$$

(18) The hand is at the 12 on the clock.
 $360^\circ \div 12 = 30^\circ$ (degrees per # on clock face)

(a) If the hand were rotated 90° clockwise, at what number would it point?

$$\frac{90^\circ}{30^\circ} = 3$$

(b) If it were rotated 150° clockwise, and then 30° counter-clockwise, at what number would it point?

$$150^\circ - 30^\circ = 120^\circ$$

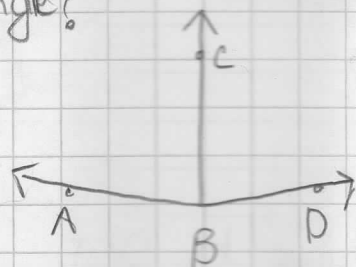
$$\frac{120^\circ}{30^\circ} = 4$$

19 $\angle ABC \cong \angle CBD$

if $\angle ABC = \left(\frac{3x}{2} + 2\right)^\circ$ and

$\angle CBD = (2x - 29\frac{1}{4})^\circ$

is $\angle ABD$ a straight angle?



$$\frac{3x}{2} + 2 = \frac{4x}{2} - 29.25$$

$$2 + 29.25 = \frac{1}{2}x$$

$$\frac{31.25}{.5} = \frac{.5x}{.5}$$

$$62.5 = x$$

$$\angle CBD = 2(62.5) - 29.25$$

$$= 125 - 29.25$$

$$= 95.75^\circ$$

if $\angle ABC = \angle CBD$
then $\angle ABC + \angle CBD$

$$= 95.75 + 95.75 = 191.5$$

which is greater than 180°

so, no $\angle ABD$ is not straight

(20) Change $15\frac{2}{9}^\circ$ to deg, min, & sec.

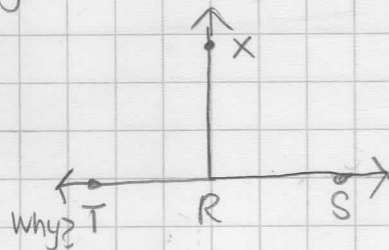
$$15^\circ \frac{2}{9} \cdot \frac{60}{1} = 13.\bar{3}$$

$$15^\circ \quad 13' \quad \frac{3}{10} \cdot \frac{60}{1} = 18$$

$$\boxed{15^\circ \quad 13' \quad 18''}$$

(21) Given: $\angle TRS$ is a straight angle
 $\angle TRX$ is a right angle
 $\angle TRS = 2x + 5y$
 $\angle XRS = 3x + 3y$

oops!



def of straight angle
 $(180^\circ - 90^\circ) = 90^\circ$

$$\text{If } \angle TRX \text{ is } 90^\circ \quad \angle XRS = 90^\circ$$

$$2x + 5y = 180$$

$$3x + 3y = 90 \leftarrow \text{solve for } x$$

$$3x = 90 - 3y$$

$$x = 30 - y \leftarrow \text{substitute}$$

$$x = 30 - 40$$

$$\boxed{x = -10}$$

$$2(30 - y) + 5y = 180$$

$$60 - 2y + 5y = 180$$

$$60 + 3y = 180$$

$$3y = 120$$

$$\boxed{y = 40}$$

(23) Change $72^{\circ}22'30''$ to degrees

$$72^{\circ} 22 \frac{30}{60}'$$

$$72^{\circ} 22.5'$$

$$72^{\circ} \frac{22.5}{60}$$

$$72.375^{\circ}$$

$$72 \frac{375}{1000} = 72 \frac{3}{8}$$

(divide numerator
& denominator by
125)